

Privacy Preserving Informative Association Rule Mining

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ABSTRACT

Privacy preserving data mining has two major directions: one is the protection of private data, i.e., data hiding in the database whereas another one is the protection of sensitive rule (Knowledge) contained in data known as knowledge hiding in the database. This research work focuses on protection of sensitive association rule. Corporation individual & other may get mutual benefit by sharing their data, but at the same time, they would like to be sure that their sensitive data remains private or not disclosed, i.e., hiding sensitive association rules. Approaches need to be given sensitive association rule in advance to hide them, i.e., mining is repaired. However, for some application pre-process of these sensitive association rules is combined with hiding process when predictive items are given, i.e., hiding informative association rule set. In this work, we propose two algorithms ISLFASTPREDICTIVE, DSRFASTPREDICTIVE to hide informative association rule with n-items. Earlier work hid 2-item association rules. Algorithms proposed in the paper execute faster than ISL & DSR algorithms prepared earlier as well as a side effect have been reduced. ISLFASTPREDICTIVE and DSRFASTPREDICTIVE algorithms work better as database scans are reduced since transaction list of elements is used in algorithms, i.e., a list of the transaction which supports itemsets and selection of transactions are done on the basis of presence of frequent itemsets.

Keywords

Informative Association Rules, Knowledge Hiding in Database, Frequent Itemset, Privacy-Preserving Data Mining, Sensitive Association Rules

1. INTRODUCTION

Data Sharing can bring many benefits for business collaboration as well as research. However, owners like to hide their sensitive data/Information before sharing their database for mining.[13, 19, 34] reflects the requirement of preserving the privacy with shared databases. Benefits of data sharing come from the business world. For hiding sensitive data, various transformation methods have been discussed in [1, 2, 3, 4, 5, 7, 23]. Hiding sensitive knowledge, i.e., association rules were first discussed in [8, 10]. Approaches for hiding sensitive association rules falls into categories like data distortion [35, 24, 25, 29, 20, 36], Data Blocking [31], Border-Based [32, 12], Data Reconstruction [14, 9, 40, 15] and cryptography approaches [22, 42]. Performance is a major concern with hiding association rules [21, 26, 28, 27, 44]. [42] presents a novel approach to hide sensitive rules with limited side effects. [33] throws light on the devel-

opment of techniques which are under the knowledge-hiding that relates to the association rule-mining task. [11] extends the work to spatial data. [41] describes the measures that can be used with association rule hiding. [43] hides rules by transactions adding or removing. [38] works on multiple tables.

2. INFORMATIVE ASSOCIATION RULE SETS

Association Rule Mining was introduced earlier in 1993. In association rule mining with market basket data, a set of items is defined as $I = \{I_1, I_2, I_3, \dots, I_n\}$. The itemsets of size one from these sets are called 1-itemsets, itemsets of size two are called 2-itemsets, and similarly, itemsets of size k is called k-itemsets. In market basket data, the database contains transactions where each transaction represents a set of items purchased in a particular transaction. An association rule is represented as $A \rightarrow B$ where A and B are itemsets which is a subset of I having support and confidence greater than user-specified support and user-specified confidence. For example, Pen \rightarrow Paper with support 80% and confidence 90% implies that Pen and Paper both are present in 80% of total transactions and 90% is the case whenever Pen is present, Paper is also present. So,

$$Support(A \rightarrow B) = \frac{Support(A \cap B)}{|D|} \quad (1)$$

$$Confidence(A \rightarrow B) = \frac{Support(A \cap B)}{Support(A)} \quad (2)$$

Support is used for removing an uninteresting rule as low support rule occur just by chance and confidence provides the reliability of an association rule. Consider Database D_1 shown in Table 1 with user-defined support threshold 55% and user-defined confi-

Table 1. : Sample database D_1

Transaction.Id	Items
1	U,V,W,X
2	U,V,W
3	U,V,W
4	U,V,W,X
5	W
6	V
7	U,V,X,Y,Z

dence threshold is 80%, eight association rules get generated as shown in Table 2.

For hiding of sensitive association rules, first sensitive rules are selected from a list of rules generated and then applied to association rule hiding algorithm whereas in informative rule sets all

Table 2. : Association rules for sample databases D₁

S_No	LHS	RHS	Support	Confidence	Lift
1	{W}	→ {U}	0.57	0.8	1.12
2	{U}	→ {W}	0.57	0.8	1.12
3	{W}	→ {V}	0.57	0.8	0.93
4	{U}	→ {V}	0.71	1	1.16
5	{V}	→ {U}	0.71	0.83	1.16
6	{U,W}	→ {V}	0.57	1	1.16
7	{V,W}	→ {U}	0.57	1	1.4
8	{U,V}	→ {W}	0.57	0.8	1.12

association rules are not generated. Here only those association rules are hidden which contains predicting items on left-hand side of the rule. So while hiding the rules, they are mined from the database containing predicting items on LHS. Let suppose predicting item is V then association rules having predicting item V on the LHS are {V} → {U}, {V,W} → {U}, {U,V} → {W}. These three rules need to be hidden. So the problem of hiding sensitive information association rule sets is defined as follows:

Given a transactional database 'D' with minimum support Threshold "MST" and minimum confidence threshold "MCT", sets of association rules and predicting item sets PI, then all the sensitive association rules are identified as $X \rightarrow Y$ where $X \subseteq PI$, and non sensitive rules are $Z \rightarrow Y$ where $Z \not\subseteq PI$, so sensitive rules need to be hidden and non sensitive rules does not be affected as much as possible.

In [39], two algorithms are proposed to hide information rule sets but side effects can be reduced by selecting the candidate transaction as the one having least number of frequent itemsets belong to it as well as performance can be enhanced by using Transaction ID List of items.

In this paper, two algorithms are presented which are the enhancement of work done in [39, 37] to improve the performance as well as to reduce the side-effect.

3. PROPOSED ALGORITHMS

A sensitive association rule can be hidden by

- Reducing the support of rule by either decreasing the support of LHS or decreasing the support of RHS
- Reducing the Confidence of Rule by either increasing the support of LHS or decreasing the support of the rule.

This work presents two algorithms, viz. ISLFASTPREDICTIVE, DSRFASTPREDICTIVE. In ISLFASTPREDICTIVE and DSRFASTPREDICTIVE algorithms, the TIDList of items has been used which greatly improves the performance of the algorithm. The logic behind the ISLFASTPREDICTIVE algorithm is to hide sensitive association rules by reducing the support of rule containing predicting item by increasing the support of LHS of the rule. In DSRFASTPREDICTIVE algorithm, the logic is to hide sensitive association by reducing the support of RHS of rule till support of confidence of the rule falls below a threshold. Algorithms select candidate transactions to be modified on the basis of a number of frequent itemsets present in it in increasing order. The algorithms are shown in algorithm 1 and algorithm 2.

4. EXAMPLES

This section presents two examples which step by step represents the action of algorithms as well as highlights the benefit of the proposed approach. Examples shown below also examine the output of the algorithms presented in [39].

Example 1:

Consider the database D₁ and select the predicting item V and

input : Database, Set of Predicting items

output: Modified database to hide Informative association rules

```

1 Find all frequent Itemsets ( $F_{sets}$ );
2 foreach Predicting item  $I \in$  Predictingitem do
3   foreach item  $Y \subseteq I$  do
4     if  $Y \notin F_{sets}$  then
5       Predictingitem = Predictingitem- {I};
6       Break;
7     end
8   end
9 end
10 foreach  $X \in$  Predictingitem do
11   Compute confidence of rule AR where  $Conf(AR) \geq$ 
    MinConf and AR is of form  $X \rightarrow Y$  i.e. Predicting item
    is on L.H.S.;
12   foreach rule AR having  $Conf(AR) \geq MinConf$  do
13     LhsList = GenerateList(X);
    // List of transactions containing
    itemset x
14     RhsList = GenerateList(Y);
    // List of transactions containing
    itemset y
15     Rule = LhsList  $\cap$  RhsList;
16     NoofModificationRequired =  $\frac{|Rule| * 100}{MCT - |LhsList|}$ ;
17     CandidateTransactionToBeModified = (T - RhsList)
     $\cap$  (T - LhsList);
    // List of transactions which does not
    support RHS and partially or no
    support for LHS
18     if  $|CandidateTransactionToBeModified| <$ 
    NoofModificationRequired then
19       Print ("ISLFASTPREDICTIVE will not work
    for hiding this rule");
20     end
21     else
22       Sort (CandidateTransactionToBeModified, by =
    presence no of frequent item sets);
23       for  $k \leftarrow 1$  to NoofModificationRequired do
24         Pick a Transaction T from
    CandidateTransactionToBeModified;
25         Pick a item i from X with least presence in
    number of frequent item sets;
    // Pick item from left-hand side
    of sensitive association rule
26         SetToOne (T,i);
27       end
28     end
29   end
30 end

```

Algorithm 1: ISLFASTPREDICTIVE Algorithm

also the maximum size of an itemset is taken as two just to compare the result with the algorithms presented in [39]. DSR algorithm [39] hides the sensitive association rule $V \rightarrow U$ successfully but hides five nonsensitive rules as shown in Table 3. DSRFASTPREDICTIVE algorithm proposed in the paper successfully hides the sensitive rule $V \rightarrow U$ and also no ghost rule generated and no rule lost. ISL algorithm [39] and ISLFASTPREDICTIVE algorithm successfully hide the sensitive rule without any side-effects.

Example 2:

Consider the database D₂ shown in Table 4 with MST=55% and MCT=80%. Let the predicting item be "B" and considering maximum 2-itemset then sensitive rule $B \rightarrow A$ needs to be hidden.

input : Database, Set of Predicting items
output: Modified database to hide Informative association rules

```

1 Find all frequent Itemsets ( $F_{sets}$ );
2 foreach Predicting item  $I \in$  Predictingitem do
3   foreach item  $Y \subseteq I$  do
4     if  $Y \notin F_{sets}$  then
5       Predictingitem = Predictingitem- {I};
6       Break;
7     end
8   end
9 end
10 foreach  $X \in$  Predictingitem do
11   Compute confidence of rule AR where  $Conf(AR) \geq$ 
    MinConf and AR is of form  $X \rightarrow Y$  i.e. Predicting item
    is on L.H.S.;
12   foreach rule AR having  $Conf(AR) \geq MinConf$  do
13     LhsList = GenerateList(X);
        // List of transactions containing
        itemset x
14     RhsList = GenerateList(Y);
        // List of transactions containing
        itemset y
15     Rule = LhsList  $\cap$  RhsList;
16     NoofModificationRequired = Min(
        |Rule| -  $\frac{TotalNumberofTransaction * MST}{100}$ ,
        |Rule| -  $\frac{|LhsList| * MCT}{100}$ );
17     CandidateTransactionToBeModified = RhsList  $\cap$ 
        LhsList;
        // List of transactions which fully
        support RHS and LHS
18     Sort(CandidateTransactionToBeModified, by =
        presence no of frequent item sets);
19     for  $k \leftarrow 1$  to NoofModificationRequired do
20       Pick a Transaction T from
        CandidateTransactionToBeModified;
21       Pick a item i from Y with least presence in
        number of frequent item sets;
        // Pick item from right-hand side of
        sensitive association rule
22       SetToZero(T,i);
23     end
24   end
25 end

```

Algorithm 2: DSRFASTPREDICTIVE Algorithm

Table 3. : Rule lost after the application of DSR algorithm on D_1

S_No	LHS	RHS	Support	Confidence	Lift
1	{W}	\rightarrow {U}	0.57	0.8	1.12
2	{U}	\rightarrow {W}	0.57	0.8	1.12
3	{V}	\rightarrow {U}	0.71	0.83	1.16
4	{U,W}	\rightarrow {V}	0.57	1	1.16
5	{V,W}	\rightarrow {U}	0.57	1	1.4
6	{U,B}	\rightarrow {W}	0.57	0.8	1.12

ISL algorithm [39] hides the sensitive association rule with one lost rule, i.e., one nonsensitive rule gets hidden whereas proposed ISLFASTPREDICTIVE algorithm successfully hides sensitive association rule without any side-effect. DSR [39] and DSRFASTPREDICTIVE algorithm both hides sensitive rule with five lost rules.

So, it is evident from both examples that it is better sometimes to select candidate transaction as the one which contains the least

Table 4. : Database D_2

Transaction_Id	Items
1	ABCD
2	ABC
3	ABC
4	ABCD
5	C
6	B
7	BCDEF

number of frequent itemsets. Approach gets performance improved by using Transaction ID List. In ISL and DSR algorithms lot of database scans are required to execute the algorithm, but in proposed approach, no database scans are needed in hiding part of algorithm since while mining the association rules, transactions list of frequent itemsets has been generated and will be used in later part of the algorithm.

5. EXPERIMENTAL VALIDATION

We have performed performance evaluation experiments on a PC with a core-i3 processor with 3 GB RAM running on Ubuntu-16.04 Operating System and the language used for implementation is R Language [30] and package used for working in R is "arules" [16, 18, 17]. The datasets used in the evaluation trials are generated using IBM synthetic data generator [6]. The database size employed in the data set range from 10K to 100K with average transaction length, $ATL = 5$, and a total number of items is 50 and number of predicting item is 2. The minimum support threshold picked is 4% & minimum confidence threshold picked is 20%. To evaluate the performance of the algorithms following effects are considered:

- Time Effects.
- Side Effects.

For Time Effects, we are considering the CPU time/running time to run ISLFASTPREDICTIVE, DSRFASTPREDICTIVE to hide sensitive association rules (AR_H) selected from the set of Association Rules generated (AR) containing the predicting item on LHS. For Side Effects, we measured Rule Hiding Failure, Rule Falsely Generated (Ghost Rules) and Rules Falsely Hidden (Lost Rules). The Rule Hiding Failure Side Effect counts the number of sensitive association rules; algorithm fails to hide. Rule Falsely Generated (Ghost Rules) side effect counts the number of rules that were not available with the original dataset, but after the modifications performed by the algorithm, the Rule appears. The Rules Falsely hidden (Lost Rules) side effect counts the number of nonsensitive rules hidden because of the data distortion process. ISLFASTPREDICTIVE algorithm is compared with ISL [39] concerning running time of the algorithm and various side effects. DSR algorithm [39] is compared with DSRFASTPREDICTIVE concerning running time of the algorithm and various side effects. All the graphs plotted to represent the average of 10 iterations of experiments.

Fig. 1, 2, 3 and 4 accounts for the Hiding Failure, Lost Rule, Ghost Rule and CPU Time of ISLFASTPREDICTIVE and ISL against various database sizes ranging from 10K to 100K respectively. Fig. 1 represents the number of rules algorithms ISL and ISLFASTPREDICTIVE fail to hide. The graph is shown using percentage because since we performed experiments with different database size for ten iterations and every time two arbitrary predicting items are selected for which informative rules to be hidden. So, the count of a number of a sensitive association rule is different each time and graph represent the average of 10 iterations. It is deceptive from the Fig. 1 that ISLFASTPREDICTIVE algorithm perform better in comparison to ISL concerning hiding failure side-effect. These algorithms sometimes fail to hide

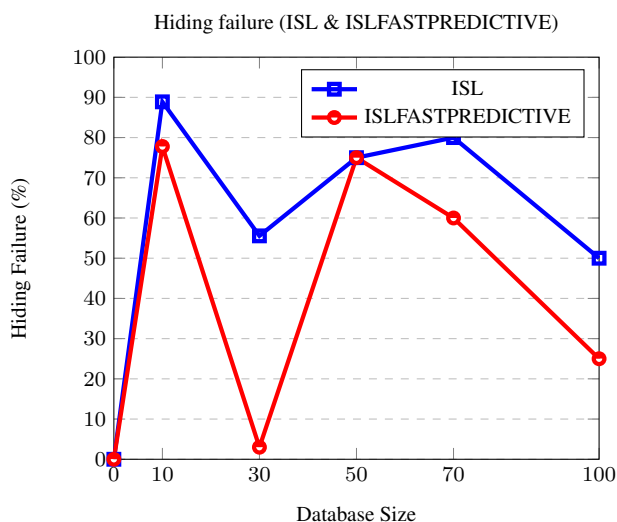


Fig. 1: Hiding failure (ISL & ISLFASTPREDICTIVE)

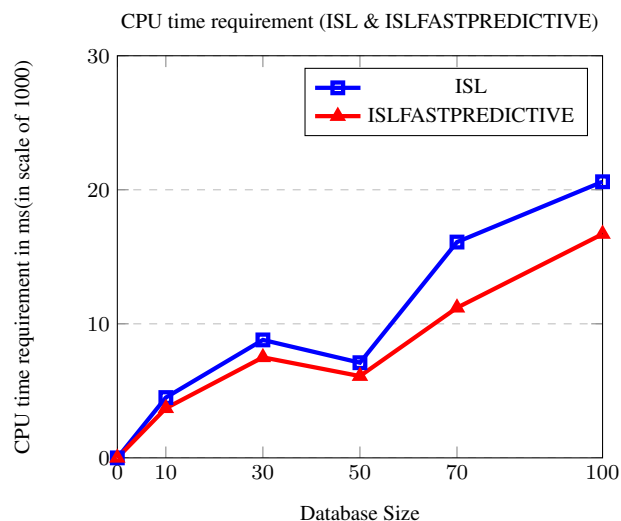


Fig. 4: CPU time requirement (ISL & ISLFASTPREDICTIVE)

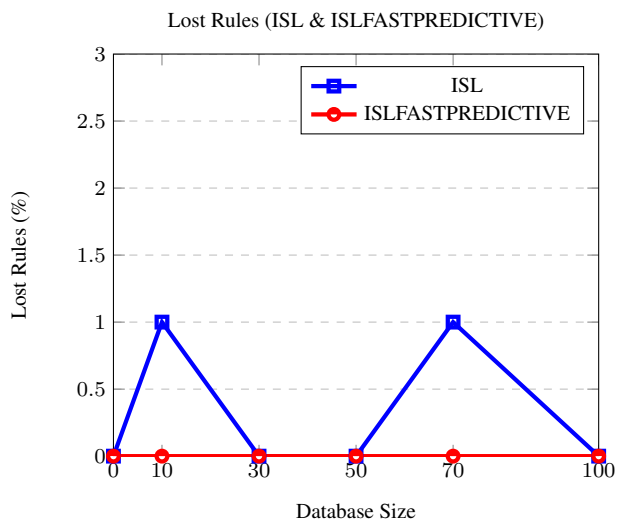


Fig. 2: Lost Rules (ISL & ISLFASTPREDICTIVE)

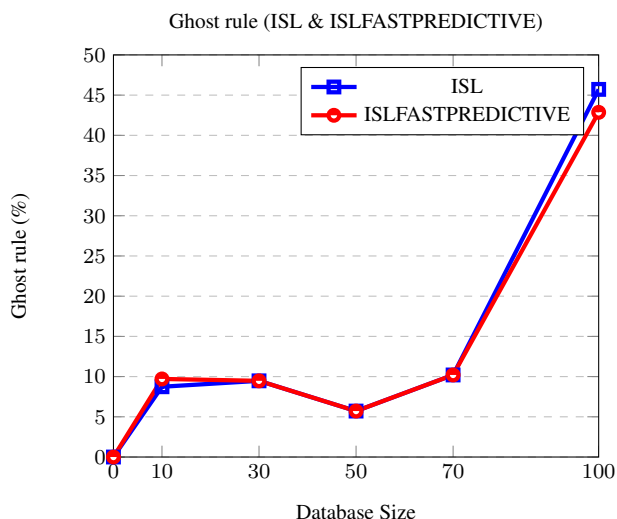


Fig. 3: Ghost rule (ISL & ISLFASTPREDICTIVE)

all sensitive association rules. Fig. 2 represents the percentage of lost rules generated by taking an average of 10 iterations of experiments. From Fig. 2, it is evident that lost rules count is reduced since transactions selected for modifications are the ones which contain the least number of frequent itemsets, so lost rule count is reduced. Fig. 3 represents the percentage of ghost rules generated by taking an average of 10 iterations of experiments. As of Fig. 3, it is clear that the number of ghost rules is reduced by a small fraction, but no appreciable difference is identified. In general, it can be said both algorithms almost perform similarly for ghost rule side effect, results are better with hiding failure and lost rules count. Also, results with proposed approach can be better when the maximum transactions to be modified are of all the same length, and there are such transactions where a number of frequent itemsets presence is very less. Fig. 4 shows the comparison of running time with ISL and ISLFASTPREDICTIVE algorithm. As it is very clear from the Fig. 4, that ISLFASTPREDICTIVE algorithm takes less time as compared to ISL. ISL scans database multiples times which increases the time requirement of the algorithm, and it becomes too high as the database size increases. ISLFASTPREDICTIVE algorithm is based on the Transaction Id list of the itemsets which already gets generated during the mining of association rules, so there are no multiple scans of the database in ISLFASTPREDICTIVE algorithm. Hence, the performance is far better with ISLFASTPREDICTIVE algorithm.

DSRFASTPREDICTIVE algorithm is compared with DSR [39] concerning running time of the algorithm and various side effects. All the graphs plotted to represent the average of 10 iterations of experiments. Fig. 5, 6, 7 and 8 accounts for the Hiding Failure, Lost Rule, Ghost Rule and CPU Time of DSRFASTPREDICTIVE and DSR against various database sizes ranging from 10K to 100K respectively. Hiding Failure is 0 with both DSR and DSRFASTPREDICTIVE algorithm. Graphs suggest that DSRFASTPREDICTIVE algorithm performs better with both ghost rule and lost rule side-effect in comparison to DSR and the best result is with lost rule and running time of the algorithm.

6. SUMMARY OF COMPARISON BETWEEN ISL, DSR, ISLFASTPREDICTIVE & DSRFASTPREDICTIVE ALGORITHMS

- (1) ISL algorithm start hiding process before checking the feasibility of approaches so many times if algorithm fails to hide certain rules, a lot of computation gets wasted, and the

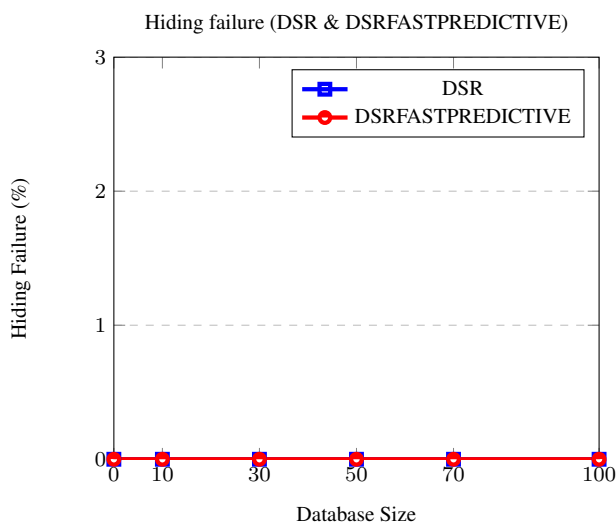


Fig. 5: Hiding failure (DSR & DSRFASTPREDICTIVE)

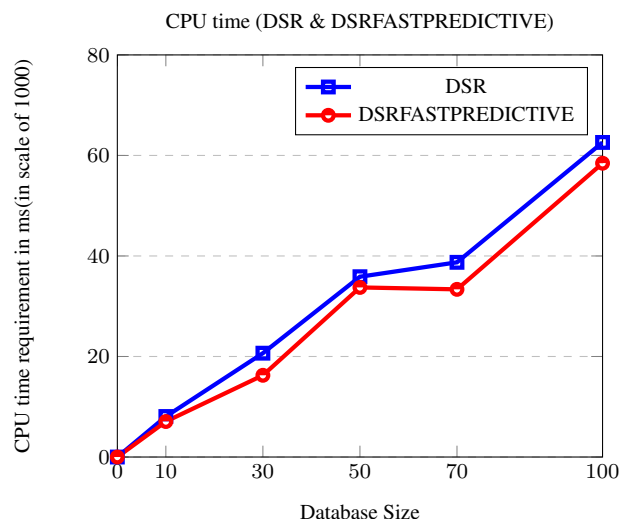


Fig. 8: CPU time requirement (DSR & DSRFASTPREDICTIVE)

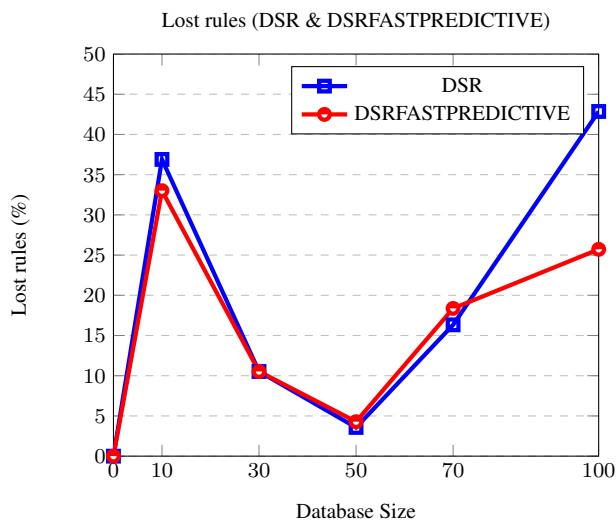


Fig. 6: Lost rules (DSR & DSRFASTPREDICTIVE)

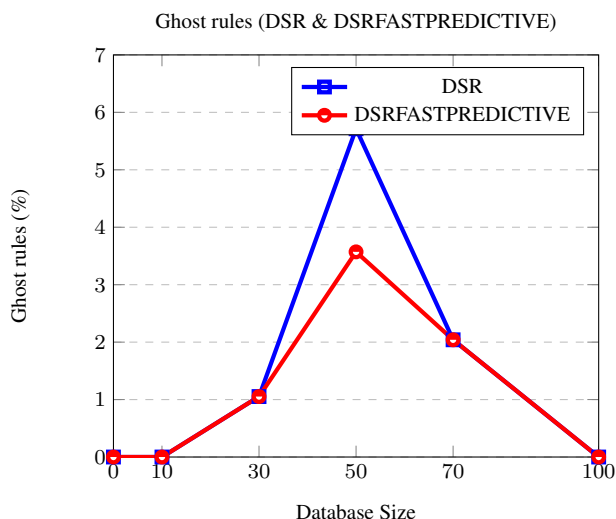


Fig. 7: Ghost rules (DSR & DSRFASTPREDICTIVE)

database is modified and being rolled back as a side-effect. In proposed approach algorithm first checks whether the approach can hide a particular rule, i.e., the feasibility of the approach is verified first which helps in reducing the computation and rollback of modifications.

- (2) ISL and DSR algorithms are designed in such a way that it can be used for hiding informative rules where length is two, but proposed approach takes any number of length of informative association rules.
- (3) ISL and DSR algorithms give priority to transactions on the basis of length of transactions whereas the ISLFASTPREDICTIVE and DSRFASTPREDICTIVE algorithm give priority to transactions on the basis of a number of frequent itemsets present in it which helps in reducing the side effect. ISL and DSR algorithm running time is high because of multiple scans of database whereas ISLFASTPREDICTIVE and DSRFASTPREDICTIVE perform better since transactions list of frequent itemsets is utilized in hiding process.

7. CONCLUSION

This paper proposes two new algorithms based on transaction list of frequent itemsets prepared while mining of association rules containing predictive items. The experimental result shows the fruitfulness of the approach. Experiments suggest that proposed approach enhances ISL and DSR algorithm regarding running time but at the same time side effects have been reduced. After experimenting with a wide range of standard datasets as well as real datasets we have come to the conclusion that approaches performed much better when there are lots of transaction of the same length since previous approaches select transactions to be modified on the basis of length whereas proposed approaches modify on the basis of the count of frequent itemsets. This can be further optimized to generate much better results.

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