Improved Grid Connected PV System based on SVPWM Inverter and using P-V Optimal Slope MPPT Technique

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ABSTRACT
This work proposes a Grid-Connected Photovoltaic Generation System (PV-GCGS) with a new and simple Maximum Power Point Tracking (MPPT). The system is composed of two stages: the short circuit current sensor stage and the dc-ac conversion stage that is a three phase Voltage Source Inverter (VSI) with space vector modulation (SVPWM) technique. The adopted MPPT technique calculates the phase angle between the inverter voltage and grid voltage to determine the optimal slope of the power load line which corresponds to the Maximum Power Point (MPP) of PV generator. The whole components of the adopted MPPT technique (Cdc conductance, Lf leakage inductance of transformer, transformer ratio and SVPWM characteristics) are designed to meet the constraints of performance and grid integration. A closed-loop controller is proposed to regulate the inverter voltage amplitude to be equal to the grid voltage in order to minimize the reactive power consumed by the transformer leakage reactance. The results are validated by simulation in the Matlab-Simulink environment.

Keywords
MPPT, short circuit-current, Grid-Connected Photovoltaic Generation System, reactive power, harmonic analysis

1. INTRODUCTION
In recent years, power generation from solar PV has known a rapid growth. It expanded by 50% per year worldwide over the last decade, reaching almost 100 TWh in 2012 [1]. Even though the deployment of photovoltaic systems has been increasing steadily for the last 20 years, solar technologies still suffer from some drawbacks that make them poorly competitive on an energy market dominated by fossil fuels: high capital cost, modest conversion efficiency, and intermittency. From a scientific and technical viewpoint, the development of new technologies with higher conversion efficiencies and low production costs is a key requirement for enabling the deployment of solar energy at a large scale [2]. To improve competitiveness of the PV generation, several research works have been made either to improve the efficiency of PV panels either to improve the power electronics interface. In the field of power electronics, two aspects are considered to improve competitiveness. In the first aspect, several MPPT algorithms are developed to maximize the output power from PV array [3-4]. In the second aspect, the use of PWM inverters and filters make it possible to improve quality of the energy injected into the grid [5-6]. These two aspects are related between them. Therefore to have a better competitiveness, these both aspects must be taken into consideration. The goals are: i) the proposal of grid connected PV system which uses a P-V optimal slope MPPT technique ii) the design of the whole PV-GCGS components to meet the constraints of efficiency and power quality.

This paper is organized as follows. In section 2, we briefly describe classical MPPT techniques. Section 3 presents and discusses the proposed system and its MPPT. Modeling and design of the adopted PV-GCGS are presented in sections 4 and 5. Simulation results are given in section 6. Finally, Section 7 outlines the conclusion.

2. CLASSICAL MPPT TECHNIQUES
2.1 Perturbation and Observation (P&O)
This technique reaches the maximum power point of PV panels using repeating sequences of perturbing, observing and comparing the power generated by the PV panels. It is widely used in PV systems because of its simplicity and easy implementation. However, it presents drawbacks such as slow response speed, oscillation around the MPP in steady state, and even tracking in wrong way under rapidly changing atmospheric conditions.

2.2 Incremental Conductance
This technique is also widely applied in the MPPT controllers. It is based on comparing the incremental conductance to the instantaneous conductance of the PV panels. The maximum PV power output can be reached when these two quantities are equal. The main advantage of this algorithm over the P&O method is its rapidity to track the maximum power point of the PV panels.

2.3 Fractional Open-Circuit Voltage
This technique is based on the approximate linear relationship between the MPP voltage ($V_{MPP}$) and the open circuit voltage ($V_{OC}$), which varies with the irradiance and temperature [7]. The $V_{MPP}$ is calculated after measuring the open-circuit voltage of the PV panels by the following relationship:

$$V_{MPP} \approx M_v \times V_{OC}$$

Where $M_v$ is a constant of proportionality, it depends on the characteristics of the PV panels used and environmental data (temperature and irradiation). According to [7] the constant $M_v$ is between 0.71 and 0.78.
2.4 Fractional Short-Circuit Current

The same reasoning as fractional open circuit but this time is applied to the current. Current corresponding to the MPP is deduced from the measurement of the short-circuit current ($I_{SC}$) by the following approximate linear relationship:

$$I_{MPP} = M_c \cdot I_{SC}$$  \hspace{1cm} (2)

The proportional parameter $M_c$ is approximately equal to 0.92 [8].

3. PROPOSED PV SYSTEM

3.1 Architecture of the proposed PV system

The proposed technique is based on the determination of the optimal slope of the power load line which corresponds to the MPP of PV generator. It requires only the measurement of the short-circuit current of the PV generator and it reaches the MPP of the PV generator with the first test and without iteration by adjusting the phase angle between the inverter voltage and grid voltage. The considered PV system (fig.1) is composed of the following stages: PV generator, short-circuit current sensor of PV generator, SVPWM inverter, and matching transformer. Amplitude modulation index and frequency modulation index of SVPWM inverter are noted $m_a$ and $mf$. Transformer ratio is noted $m$. We kept the transformer for its advantage to eliminate the leakage current, to filter the injected currents in the grid (One contribution of this work) and to adjust voltage levels. The size of the transformer is compensated by the lack of filtering inductances, because the transformer’s leakage inductances are used for filtering the currents injected into the grid.

![Proposed PV Grid-Connected Generation System](image)

3.2 Proposed MPPT technique

Inverter-grid link can be modeled by the single line diagram shown on fig. 2. Power-voltage characteristic of the load, i.e. grid connected inverter, is then a line whose expression is:

$$P_{load} = \frac{3}{4} m_a m_v \cdot V_{ut} \cdot \sin \theta \cdot V_{pv}$$  \hspace{1cm} (3)

Where:

- $V_{ut}$: Magnitude of line to line voltage grid.
- $V_{pv}$: PV generator voltage.
- $X = 2\pi.F.L$: Transformer’s leakage reactance.
- $F$: Grid’s frequency.
- $\theta$: the phase angle between the inverter voltage and grid voltage.

The slope of this characteristic is:

$$S_{sys} = \frac{3}{4} m_a m_v \cdot \sin \theta$$  \hspace{1cm} (4)

![Inverter-Grid link Model](image)

Fig 2: Inverter-Grid link Model.

Fig.3 shows the V-I and V-P curves of PV generator. In the V-P plan, the MPP is the intersection of the P-V curve of the PV generator and the load line (inverter- grid) having an optimal slope:

$$S_{op} = \frac{P_{MPP}}{V_{MPP}} = \frac{M_{CC} m_v V_{CO}}{m_v V_{CO}}$$  \hspace{1cm} (5)

To extract the maximum power from the PV generator, it is necessary that the load line slope is equal to the optimal slope. Thus:

$$\frac{3}{4} m_a m_v \cdot \sin \theta = M_c I_{CC}$$  \hspace{1cm} (6)

Therefore the optimal slope can be achieved by controlling $ma$, $m$ and $\theta$. This approach was already presented in [9]. In [10], $\theta$ is used to determine the optimal slope and the other parameters are taken constants, and calculated to satisfy the requirements of quality and grid connection. In this work $ma$ is also controlled in order to achieve the optimal slope and to satisfy the requirements of quality and grid connection. A SVPWM is used to meet all these requirements.

To extract the maximum power from the PV generator, the fundamental voltage generated by the VSI based on SVPWM control is phase shifted to the mains voltage by:

$$\theta = asin\left(\frac{3}{4} \frac{X}{m_a m_v} M_c I_{SC}\right)$$  \hspace{1cm} (7)

This MPPT technique requires the measurement of short-circuit current and the estimate of current factor ($M_c$).

3.3 $I_{sc}$ sensor stage

This stage is used to measure the short-circuit current of the PV generator and operates in more favorable conditions than in the case of the boost in conventional systems. Indeed, the frequency of the power switches of this stage is less than 50Hz in the proposed system while it exceeds 20 KHz in the conventional systems. Also, this stage saves the inductance of boost. Consequently, the benefits of this stage are reducing losses due to the switching of the power switches (low switching frequency), minimizing size and cost.

3.4 Current proportional parameter estimation

The effectiveness of the proposed MPPT depends on the value
assigned to $Mc$ particularly its dependence on climatic conditions. In [8], $Mc$ is estimated under various conditions of temperature, illumination and for different PV panels. This reference indicates that the current factor is always constant, even if the temperature and illumination varies.

$$PPV, IPV = ISC \times V_{PV}$$

$$P_{load} - \theta_{optimal} \leq P_{load} - \theta_1$$


\[ F_{Pr, V_r/V_s=1} \]

\[ F_{Ps, V_r/V_s=1} \]

\[ F_{Ps, V_r/V_s=0.8} \]

\[ F_{Pr, V_r/V_s=0.8} \]

\[ \theta (\text{degree}) \]

\[ \text{PF} \]

\[ \text{P}_{\text{load}} - \theta_2 > \theta_1 \]

\[ P_{load} - \theta_1 \]

\[ V_{PV} \]

\[ \theta_1 \leq \theta \leq \theta_2 \]

\[ \text{P}_{\text{load}} \]

\[ \text{P}_{\text{load}} - \theta_1 \]

\[ \text{P}_{\text{load}} - \theta_2 \]

\[ \text{P}_{\text{load}} - \theta_0 \]

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\[ \text{P}_{\text{load}} \]

\[ \text{P}_{\text{load}} - \theta_1 \]

\[ \text{P}_{\text{load}} - \theta_2 \]
IH(mf) represents the amplitude of the total harmonic currents of the first 200 packets in p.u (voltage reference is \( V_{PV}/2 \) and current reference is \( (V_{PV}/2)/X \). Fig 7.a and 7.b show \( IH \) vs \( mf \) and THDI vs \( \theta \) respectively.

5. PV SYSTEM DESIGN

The purpose of this section is to determine the parameters of all components of the proposed PV system to meet the following specifications:

- Power: \( P_{min} \leq P_{sys} \leq P_{max} \)
- Power factor: \( PF \geq PF_{min} \)
- Power quality: \( THDI \leq THDI_{max} \)
- Best performance, cost and size are possible.

5.1 Voltage control loop

From fig.5 the reactive power consumed by the transformer leakage reactance is minimal when:

\[
V_r/V_{Pv} = 1
\]

Knowing that: \( V_r = m_a V_{mpp} \) and \( V_{Pv} = m_a V_{ut} \) (constant) and considering (15) the \( V_{mpp} \) range can be expressed as:

\[
\frac{m_a V_{ut}}{m_{amin}} \leq V_{mpp} \leq \frac{m_a V_{ut}}{m_{amax}}
\]

5.2 Choice of \( ma \) and \( m \)

The MPP voltage varies according to the climatic conditions (illumination and temperature) variation. So to calculate the transformer ratio an interval of MPP voltage variation is chosen:

\[
V_{Pvmin} \leq V_{MPP} \leq V_{Pvmax}
\]

So for (25) remains satisfied, it is necessary that the following expression must be fulfilled when the system operates at maximum power \( P_{max} \):

\[
\frac{3}{2} \left( \frac{m_a V_{Pv}}{2} \right)^2 \sin(\theta_{max}) \geq \frac{P_{max}}{X_{max}}
\]

So:

\[
X \leq X_{max} = \frac{3}{2} \left( \frac{m_a V_{Pv}}{2} \right)^2 \sin(\theta_{max}) \frac{1}{P_{max}}
\]

Initially \( mf \) is chosen arbitrarily and the corresponding \( IH \) is determined from the curve in fig.7a.

To meet the \( THDI \) specification and substituting (13) into (14) yields:

\[
sin \left( \frac{\theta}{2} \right) \geq \frac{1}{2} \frac{IH(mf)}{THDI_{max}}
\]

So it is necessary to set a minimum value of \( \theta \):
\[ \theta \geq \theta_{\text{min}} = 2 \cdot \arcsin \left( \frac{1}{2} \frac{m_f}{\text{TTHD}_{\text{max}}} \right) \]  
(29)

For (29) remains satisfied, it is necessary that the following expression must be fulfilled when the system operates at minimum power \( P_{\text{min}} \) and taking into account (15):

\[ \frac{3}{2} \left( \frac{m_a V_{\text{PV}}}{2} \right)^2 \sin \left( \frac{\theta_{\text{min}}}{x} \right) \leq P_{\text{min}} \]  
(30)

Substituting (29) into (30) yields:

\[ X \geq X_{\text{min}} = \frac{3}{8} \left( \frac{m_a V_{\text{PV}}}{p_{\text{min}}} \right)^2 \sin \left( \frac{1}{2} \frac{m_f}{\text{TTHD}_{\text{max}}} \right) \]  
(31)

If \( X_{\text{min}} \geq X_{\text{max}} \) or the choice interval of the transformer’s leakage reactance is not sufficiently large, then it is necessary to adjust the value of \( m_f \).

Therefore the transformer’s leakage reactance should meet:

\[ X_{\text{min}} < X_{\text{tr}} < X_{\text{max}} \]  
(32)

### 5.4 Determination \( C_{\text{dc}} \)

Measuring the \( I_{\text{SC}} \) should not cause a large distortion of the DC voltage supply. The value of \( C_{\text{dc}} \) is calculated to limit the voltage drop during the operation of the \( I_{\text{SC}} \) sensor.

For the capacitor can replace the PV generator during the short-circuit without that the relative variation of its voltage exceeds \( (V_{\text{PV}}/\Delta V_{\text{PV}})_{\text{max}} \), it is necessary that:

\[ C_{\text{dc}} \geq \frac{p_{\text{PV}} \Delta I_{\text{SC}}}{2 V_{\text{PV}}} \left( \frac{1}{\Delta V_{\text{PV}}/V_{\text{PV}}} \right) \]  
(33)

\( \Delta I_{\text{SC}} \) should be sufficient for the current to be stabilized. It is determined by a return on experience \( \Delta I_{\text{SC}} = 25 \mu s \)

### 5.5 Numerical computation

The PV generator consists of four panels in series (ET-P636135).

**Table 1: Parameters and specifications of the proposed PV system**

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Maximum power (( P_{\text{MPP}} ))</td>
<td>135W</td>
</tr>
<tr>
<td>Voltage @ ( P_{\text{MPP}} ) (( V_{\text{MPP}} ))</td>
<td>17.67V</td>
</tr>
<tr>
<td>Current @ ( P_{\text{MPP}} ) (( I_{\text{MPP}} ))</td>
<td>7.67A</td>
</tr>
<tr>
<td>Short circuit current (( I_{\text{SC}} ))</td>
<td>8.41A</td>
</tr>
<tr>
<td>( V_{\text{ac}} ) and ( F )</td>
<td>220V – 50Hz</td>
</tr>
<tr>
<td>( P_{\text{max}} )</td>
<td>600W</td>
</tr>
<tr>
<td>( P_{\text{min}} )</td>
<td>60W</td>
</tr>
<tr>
<td>( V_{\text{PV}} )</td>
<td>73V</td>
</tr>
<tr>
<td>( \text{TTHD}_{\text{max}} )</td>
<td>5%</td>
</tr>
<tr>
<td>( \Delta I_{\text{SC}} )</td>
<td>25( \mu )s</td>
</tr>
</tbody>
</table>

The flowchart of fig. 9 summarizes the procedure for choosing the suitable transformer to be used to connect the PV generator-inverter to the grid.

According to the data tabl.1 and the flowchart fig.9. The calculation results are given below:
The results summarized in tab.2 shows a good agreement between theoretical and simulation results.

7. CONCLUSION

In this paper, a three phase grid-connected PV inverter with a new MPPT technique based on the determination of the P-V optimal slope of PV generator has been presented. The operating principle of the proposed MPPT technique is to adjust the phase angle between the inverter fundamental voltages and grid voltages to obtain the P-V optimal slope of the PV generator i.e. the MPP. An optimized design procedure has also been studied in this paper. Simulation results confirm the effectiveness of the proposed PV system. The proposed MPPT technique can be implemented in the PV systems with the provided design guidelines. In addition, it can further participate to the development of the PV systems. Future work will include analysis of partial shading on the proposed MPPT technique. Also experimental results will be presented.

8. REFERENCES

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